

UNIT 9 EXPONENTS REVIEW SOLUTIONS

1) Express the following using exponents.

a. $2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$

$$2^9$$

b. $\frac{1}{x}$

$$x^{-1}$$

c. $5 \cdot 5 \cdot m \cdot m \cdot n \cdot n \cdot n$

$$5^3 m^2 n^4$$

d. $\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$

$$\left(\frac{1}{2}\right)^3$$

2) Express the following without using exponents.

a. $2^3 x^2$

$$2 \cdot 2 \cdot 2 \cdot x \cdot x$$

b. 4^{-3}

$$\frac{1}{4 \cdot 4 \cdot 4}$$

c. $\left(\frac{3}{4}\right)^3$

$$\frac{3}{4} \cdot \frac{3}{4} \cdot \frac{3}{4}$$

d. x^{-5}

$$\frac{1}{x \cdot x \cdot x \cdot x \cdot x}$$

Simplify. Your answer should contain only positive exponents.

3) $3^2 \cdot 3^2 = 3^4$

4) $2^{-2} \cdot 2^4 = 2^2$

5) $(3^{-4})^2 = 3^{-8} = \frac{1}{3^8}$

6) $(3^3)^2 = 3^6$

7) $\frac{2^3}{2^{-1}} = 2^4$

8) $\frac{4^{-4}}{4^2} = 4^{-6} = \frac{1}{4^6}$

9) $2n^{-4} \cdot 3n^{-3} = 6n^{-7} = \frac{6}{n^7}$

10) $4m^3 \cdot m^2 \cdot 4m^4 = 16m^9$

11) $(r^{-3})^3 = r^{-9} = \frac{1}{r^9}$

12) $(4a^4)^2 = 16a^8$

$$13) -\frac{4x^0}{4x^2} = -1x^{-2} = -\frac{1}{x^2}$$

$$14) \frac{3n^2}{-n^3} = -3n^{-1} = -\frac{3}{n}$$

$$15) -2y^2 \cdot 4y^{-3} = -8y^{-1} = -\frac{8}{y}$$

$$16) 4m^{-2}n^2 \cdot 4m^4 = 16m^2n^2$$

$$17) (-4x^3y^0)^2 = 16x^6$$

$$18) (-x^4y^2)^3 = -x^{12}y^6$$

$$19) \frac{4x^0y^4}{-4x^{-4}} = -1x^4y^4$$

$$20) \frac{4yx^2}{2yx^0} = 2x^2y^0 = 2x^2$$

$$21) (2x^3)^3x^{-1} = 8x^9x^{-1} = 8x^8$$

$$22) \frac{4r^4 \cdot r^{-2}}{r^4} = \frac{4r^2}{r^4} = 4r^{-2} = \frac{4}{r^2}$$

$$23) \left(\frac{2x^4}{2x^2}\right)^3 = \frac{8x^6}{8x^6} = 1x^6$$

$$24) \frac{(-2a^4)^2}{a^3 \cdot -2a^4} = \frac{+4a^8}{-2a^7} = -2a$$

Simplify. Write each answer in scientific notation.

$$25) (5.8 \times 10^9)(3 \times 10^{-5}) = 1.74 \times 10^5$$

$$26) (2 \times 10^{-9})(6 \times 10^9) = 1.2 \times 10^1$$

$$27) \frac{7 \cdot 10^{12}}{2.5 \cdot 10^7} = 2.8 \times 10^5$$

$$28) \frac{8.8 \times 10^{-7}}{8 \times 10^{-1}} = 1.1 \times 10^{-6}$$

$$29) (8 \cdot 10^{-5})^4 = 4.096 \times 10^{-17}$$

$$30) (3 \cdot 10^2)^9 = 1.9683 \times 10^{22}$$

Express in scientific notation

$$31) 5,555,000,000$$

$$5.555 \times 10^9$$

$$32) 0.0072$$

$$7.2 \times 10^{-3}$$

Express in standard notation (decimal notation).

$$33) 5 \times 10^{-5}$$

$$0.00005$$

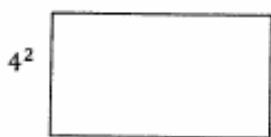
$$34) 8.35 \times 10^6$$

$$8,350,000$$

REVIEW APPLICATIONS

Find the area of the following rectangles:

1.



$$4^3 \cdot 4^2 = 4^5$$

2.



$$\begin{aligned} & \overbrace{x(3x-4)}^{3x-4} \\ & 3x^2 - 4x \end{aligned}$$

3.



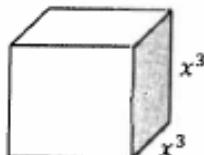
$$\begin{aligned} & \overbrace{2x^2(2x^3 + 4x)}^{2x^3 + 4x} \\ & 4x^5 + 8x^3 \end{aligned}$$

Find the volume of the following cubes:

4.

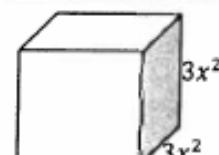
$$\begin{aligned} V &= s^3 & V &= lwh \\ & 3^2 & 3^2 & \\ & (3^2)^3 & (3^2)(3^2)(3^2) \\ & 3^6 & 3^6 \\ & \text{either } 3^6 & \text{or } 3^6 \\ & \text{or } 3^6 & \text{or } 3^6 \end{aligned}$$

5.



$$(x^3)^3 \stackrel{\text{either}}{=} (x^3)(x^3)(x^3) \quad (x^3)^3 = x^9$$

6.



$$\begin{aligned} & (3x^2)^3 = 27x^6 & (3x^2)(3x^2)(3x^2) \\ & 3^3 x^6 & 27x^6 \end{aligned}$$

EXPAND

Expand the following to simplify. SHOW WORK!

$$\begin{aligned} 7. \quad (3xy^3)^2(2x^4y^2) &= \\ (3xyyy)(3xyyy)(2xxxxyy) & \\ 18xxxxxyyyyyyy & \\ 18x^5y^8 & \end{aligned}$$

RULE

Use the rules to simplify.

$$\begin{aligned} 8. \quad (-5x^7y^2z)^4(4xy^0z^9)^3 &= \\ (-5)^4 x^{28} y^8 z^4 \cdot 4^3 x^3 z^{27} & \\ 625x^{28}y^8z^4 \cdot 64x^3z^{27} & \\ 40000x^{31}y^8z^{31} & \end{aligned}$$

9. List the elements in order from least to concentration to greatest concentration.

Elements in Seawater	Concentration (parts per million)
Sulfur	904
Chloride	1.95×10^4
Magnesium	1.29×10^3
Sodium	10,770

Sulfur, Magnesium, Sodium, Chloride
904 1290 10770 19500