

1) The frequency, F , of a vibrating guitar string is directly proportional to the square root of the tension, T , on the string and inversely proportional to the length, L , of the string.

a) Write an equation to model the frequency of a guitar string.

$$F = \frac{k\sqrt{T}}{L}$$

b) If both the tension on the string and the length are doubled, what would happen to the frequency?

Increase by factor of $\sqrt{2}$

$T = 4, L = 1$

$$F = \frac{k\sqrt{4}}{1} \Rightarrow F = k\sqrt{4}$$

$$F = \frac{k\sqrt{8}}{2} \Rightarrow \frac{2F}{2} = \frac{2k\sqrt{2}}{2} \quad F = \frac{2\sqrt{2}k}{2}$$

c) You want to modify your guitar so that you can play bass guitar. What are two ways to cut the frequency of a string in half?

Length doubled or cut tension by a factor of 4

$$\frac{2F}{2} = \frac{k\sqrt{T}}{L} \Rightarrow \frac{1}{2}$$

2) A solution is heated from 0°C to 100°C . Between 0°C and 50°C , the rate of temperature increase is $1.5^\circ\text{C}/\text{min}$. Between 50°C and 100°C , the rate of temperature increase is $0.4^\circ\text{C}/\text{min}$. What is the average rate of temperature increase during the entire heating process?

$$\text{Avg. rate} = \frac{\Delta \text{temp}}{\Delta \text{time}} = \frac{100}{158.3} = .6^\circ\text{C}/\text{min}$$

$$\text{Time} = \frac{50}{1.5} + \frac{50}{.4} = 158.3$$

3) Sharon invites the cheerleaders to support the school's dive team at their recent competition. The trip will cost \$145 per person plus \$1000 deposit.

a) Write a function to represent the cost of the trip per person.

$$f(x) = \frac{1000}{x} + 145$$

b) What is the cost per person if 5 cheerleaders go on the trip?

$$\$345.00$$

7 cheerleaders go on the trip?

$$\$287.90$$

10 cheerleaders go on the trip?

\$ 245.00

~~c) What is the increased cost for each of 10 cheerleaders to go with the dive team rather than to go with the robotics team?~~

4) A glassblower can produce a set of simple glasses in about 2 h. When the glassblower works with an apprentice, the job takes about 1.5 h. How long would it take the apprentice to make a set of glasses when working alone?

$$\begin{aligned} \text{GlassBlower} &= \frac{1}{2} \\ G+A &= 1.5 \text{ h} \\ \frac{1}{2}(1.5) + \frac{1}{x}(1.5) &= 1 \\ \frac{1.5}{2} + \frac{1.5}{x} &= 1 \\ x &= 6 \end{aligned}$$

5) Marcus and Will are painting a barn. Marcus paints about twice as fast as Will. On the first day, they have worked for 6 h and completed $\frac{1}{3}$ of the job when Will gets injured. If Marcus has to complete the rest of the job by himself, about how many additional hours will it take him?

$h = \# \text{ hours for Marcus}$ $2h = \text{Will}$

$$\left(\frac{2}{3}\right)(27) = 18$$
$$\frac{1}{h}(6) + \frac{1}{2h}(6) = \frac{1}{3}$$

$$\frac{6}{h} + \frac{6}{2h} = \frac{1}{3}$$

$$12 + 6 = \frac{2}{3}h$$

$$h = 27$$