

Solve each equation.

1. $\frac{1}{2}x^2 = -28$

2. $3x^2 + 14 = -19$

Find the values of x and y that make each equation true.

3. $6x - 2i = (-2y)i + 10$

4. $-40i + 2x = (5y)i - 12$

5. $-8y + 14i = (7x)i - 2$

Find each complex conjugate.

9. $\sqrt{3}i - 25$

10. $-5i + \frac{12}{5}$

11. $-2 - 1.5i$

Find each absolute value.

12. $|-12 + 6i|$

13. $|-7 - 4i|$

14. $\left| \frac{1}{2} + \frac{1}{2}i \right|$

Add or subtract. Write the result in the form $a + bi$.

15. $(8 - i) - (-5 - 4i)$

16. $(2 - 11i) - (10 + 6i)$

17. $\left(\frac{1}{2} + \frac{3}{4}i \right) + \left(-\frac{1}{4} - \frac{5}{4}i \right)$

Multiply or divide. Write the result in the form $a + bi$.

18. $\frac{-3 + 7i}{1 + 8i}$

19. $(-4 - 9i)(8 + 2i)$

20. $\frac{5 + i}{2 - i}$

Simplify.

21. $i^{24} - i^{13} + i^{12}$

22. $-4i^{13}$

23. $6 - 4i^{18}$

24. In a circuit, the voltage, V , is given by the formula $V = IZ$, where I is the current and Z is the impedance. Both the current and impedance are represented by complex numbers. Find the voltage if the current is $3 + 2i$ and the impedance is $4 - i$.

Challenge Problems

Evaluate and simplify.

25. $\sqrt{-8} \cdot \sqrt{-128}$

26. $\sqrt{-3} \cdot \sqrt{-2} \cdot \sqrt{-6} \cdot \sqrt{-4}$

27. $(\sqrt{-5})^2$

28. $\sqrt{-2} \cdot \sqrt{-90} \cdot \sqrt{-5}$

29. $\sqrt{-3} \cdot \sqrt{12}$

30. $(\sqrt{-2})^5$